

Computation of Oscillating Airfoil Flows with One- and Two-Equation Turbulence Models

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The ability of one- and two-equation turbulence models to predict unsteady separated flows over airfoils is evaluated. An implicit, factorized, upwind-biased numerical scheme is used for the integration of the compressible, Reynolds-averaged Navier-Stokes equations. The turbulent eddy viscosity is obtained from the computed mean flowfield by integration of the turbulent field equations. One- and two-equation turbulence models are first tested for a separated airfoil flow at fixed angle of incidence. The same models are then applied to compute the unsteady flowfields about airfoils undergoing oscillatory motion at low subsonic Mach numbers. Experimental cases where the flow has been tripped at the leading-edge and where natural transition was allowed to occur naturally are considered. The more recently developed turbulence models capture the physics of unsteady separated flow significantly better than the standard $k-\epsilon$ and $k-\omega$ models. However, certain differences in the hysteresis effects are observed. For an untripped high-Reynolds-number flow, it was found necessary to take into account the leading-edge transitional flow region to capture the correct physical mechanism that leads to dynamic stall.

Introduction

APPLICATION of Navier-Stokes methods to complex, unsteady, turbulent flows is a field of continuous interest. An example of such a flow is the massively separated flow over airfoils at high incidence or in dynamic motion. For the computation of these flowfields, application of algebraic turbulence models, such as the Cebeci-Smith¹ model, the Baldwin-Lomax² model, or the algebraic renormalization group (RNG) based model,³ becomes very complicated and often ambiguous. The source of ambiguity comes from the difficulty in defining characteristic length scales, e.g., the boundary-layer thickness required by these models. The Johnson-King⁴ model, referred to as half-equation model because it requires the solution only of one ordinary differential equation for the maximum shear stress, was proven to be quite accurate in predicting mildly separated flows where the boundary-layer thickness is well defined. The standard $k-\epsilon$ ⁵ and $k-\omega$ ⁶ two-equation turbulence models and the one- and two-equation turbulence models developed over the last few years,⁷⁻⁹ do not have these ambiguities. The more recently developed models⁷⁻⁹ also seem to show promise for massively separated flowfields. These models have been extensively tested for attached and mildly separated steady flows. The ability of these models to resolve massively separated flows, such as flow over a wing at stall, a slender body at an angle of incidence, or unsteady separated flow at dynamic stall conditions, however, has not been systematically evaluated. The objective of this investigation is to test one- and two-equation models for unsteady massively separated flows.

Some turbulence models have been tested for two-dimensional unsteady separated flows. It was found that it is advantageous to use the Johnson-King model for separated flows where nonequilibrium

effects are important. In Refs. 10-12 it was shown that, for light dynamic stall, the Johnson-King model captures flow separation better and yields improved predictions of hysteresis effects, compared with standard algebraic models. In the present investigation, however, it was found that the experimental data¹³ used for validation of fully turbulent solutions in Refs. 10 and 11 depend also on leading-edge transition, which has a significant effect on the development of the unsteady flowfield. The $k-\epsilon$ model has been compared with the Baldwin-Lomax model in Refs. 14 and 15 for dynamic motion. In a previous investigation¹⁶ an extensive evaluation of algebraic, half- and one-equation models for the prediction of dynamic stall was conducted. A single model that could predict accurately the attached unsteady flow, the light- and deep-stall regimes was not identified.

In Ref. 16 a central difference numerical procedure validated with experiments in Refs. 10 and 17 was used. It was found, however, that unsteady solutions obtained with this central differencing scheme were sensitive to grid spacing in the near-wall region and to artificial smoothing. Therefore, here the upwind-biased numerical scheme described in detail in Ref. 18 is used. One- and two-equation models are tested first for steady separated flow. The same models are then applied to compute unsteady flowfields over oscillating airfoils. The ability of one- and two-equation models to predict unsteady attached flow, the light-, and deep stall regimes is evaluated. The computed results appear to be grid independent, and no artificial smoothing is used. Finally, it is shown that the leading-edge transitional flow has a significant effect on the development of the unsteady flowfield about oscillating airfoils. The numerical scheme and the turbulence models are briefly described in the following sections.

Numerical Implementation

The conservative form of the thin-layer approximation to the compressible, Reynolds-averaged, Navier-Stokes equations for body-fitted coordinate system (ξ, η) is used. These equations are as follows:

$$\partial_t \hat{q} + \partial_\xi \hat{F} + \partial_\eta \hat{G} = Re^{-1} \partial_\eta \hat{S} \quad (1)$$

where \hat{q} is the conservative variable vector, $\hat{q} = [\rho, \rho u, \rho v, e]^T$, \hat{F} and \hat{G} are the inviscid flux vectors, and \hat{S} represents the thin-layer approximation of the viscous terms in the normal direction. In the previous equation all geometrical dimensions are normalized with the airfoil chord length c ; the density ρ is normalized with the

Presented as Paper 94-0190 at the AIAA 32nd Aerospace Sciences Meeting, Reno, NV, Jan. 10-13, 1994; received Jan. 12, 1994; revision received May 10, 1994; accepted for publication May 10, 1994. Copyright © 1994 by the American Institute of Aeronautics and Astronautics, Inc. No copyright is asserted in the United States under Title 17, U.S. Code. The U.S. Government has a royalty-free license to exercise all rights under the copyright claimed herein for Governmental purposes. All other rights are reserved by the copyright owner.

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freestream density ρ_∞ ; the Cartesian velocity components (u, v) of the physical domain are normalized with the freestream speed of sound a_∞ ; and the pressure p is normalized with p_∞ .

The following upwind-biased, factorized, iterative, implicit numerical scheme is used to compute the mean flow:

$$\begin{aligned} & [I + h_\xi (\nabla_\xi^b \tilde{A}_{i,k}^+ + \Delta_\xi^f \tilde{A}_{i,k}^-)]^p \\ & \times [I + h_\eta (\nabla_\eta^b \tilde{B}_{i,k}^+ + \Delta_\eta^f \tilde{B}_{i,k}^- - Re^{-1} \delta_\eta \tilde{M}_{i,k})]^p (\tilde{Q}_{i,k}^{p+1} - \tilde{Q}_{i,k}^p) \\ & = - \left[(\tilde{Q}_{i,k}^p - Q_{i,k}^n) + h_\xi (\hat{F}_{i+\frac{1}{2},k}^p - \hat{F}_{i-\frac{1}{2},k}^p) \right. \\ & \left. + h_\eta (\hat{G}_{i,k+\frac{1}{2}}^p - \hat{G}_{i,k-\frac{1}{2}}^p) - Re^{-1} h_\eta (\hat{S}_{i,k+\frac{1}{2}}^p - \hat{S}_{i,k-\frac{1}{2}}^p) \right] \quad (2) \end{aligned}$$

In this equation, $h_\xi = \Delta\tau/\Delta\xi$ and $\tilde{A}^\pm = (\partial\tilde{F}/\partial\tilde{Q})$, etc., are the flux Jacobian matrices. The quantities $\tilde{F}_{i+\frac{1}{2},k}$, $\tilde{G}_{i,k+\frac{1}{2}}$, and $\tilde{S}_{i,k+\frac{1}{2}}$ are numerical fluxes. The inviscid fluxes \hat{F} and \hat{G} are evaluated using Osher's¹⁹ upwinding scheme. Third-order accurate, upwind-biased numerical fluxes are computed. For the linearization of the left-hand side terms, the flux Jacobian matrices A and B are evaluated by the Steger-Warming²⁰ flux-vector splitting. The viscous fluxes $\hat{S}_{i,k+\frac{1}{2}}$ are computed with central differences.

The boundary conditions are specified as follows. On the solid surface the velocity is specified either zero for steady solutions or to the airfoil velocity for time-dependent motions. The density and pressure are obtained from the interior using first-order extrapolation. At the inflow, freestream conditions are specified for velocity and pressure, and one-dimensional Riemann invariant extrapolation is used to obtain the density. At the outflow, freestream pressure is specified, and one-dimensional Riemann invariants are used to obtain the velocities and the density from the interior.

Turbulence Models

An attractive feature of one- and two-equation models is that they can be utilized in a more straightforward manner compared with algebraic models in both structured and unstructured flow solvers, which are becoming increasingly more popular. The accuracy and the numerical robustness of these models should be further demonstrated. Among the most widely used one-equation models are the Baldwin-Barth⁷ (B-B) and the Spalart-Allmaras⁸ (S-A) models. The first model was derived from the two-equation $k-\epsilon$ model by introducing some simplifying assumptions. The Spalart-Allmaras model was developed based on dimensional analysis and empirical criteria. An advantage of the previous turbulence models compared with the algebraic and half-equation models is that they do not require evaluation of ambiguous length scales. One-equation models require numerical solution of only one partial differential equation; therefore, they are less computationally intensive compared with two-equation models. In this paper the standard versions of the Baldwin-Barth⁷ and Spalart-Allmaras⁸ models are used to compute steady and unsteady separated flows.

The most popular nonalgebraic turbulence models are two-equation eddy-viscosity models. These models solve two transport equations, one for the turbulent kinetic energy k and another one related to the turbulent length (or time) scale. Among the two-equation models, the $k-\epsilon$ model is the most widely used today. The original Jones and Launder $k-\epsilon$ model⁵ and its variants have been very successful in a large variety of different flow situations, but it also has a number of well-known shortcomings. From the standpoint of aerodynamics, the most disturbing is the lack of sensitivity to strong adverse pressure gradients. Another shortcoming of the $k-\epsilon$ model is associated with the numerical stiffness of the equations when integrated through the viscous sublayer.

The $k-\omega$ model has been developed by Wilcox⁶ to overcome the shortcomings of the $k-\epsilon$ model. This model solves one equation for the turbulent kinetic energy k and a second equation for the specific turbulent dissipation rate (or turbulence frequency) ω . The $k-\omega$ model performs significantly better under mild adverse pressure-gradient conditions than the $k-\epsilon$ model. Another strong point of the model is the simplicity of its formulation in the viscous sublayer. The model does not employ damping functions and has straightforward

boundary conditions. This leads to significant advantages in numerical stability. The $k-\omega$ model has been validated extensively^{6,21} for many flow cases with and without adverse pressure gradient. For all cases it was found to perform equally well or better than the $k-\epsilon$ model. The major shortcomings of the $k-\omega$ model are that the results of the model depend strongly on the freestream values ω_f that are specified outside the shear layer and that the model fails to predict separation for adverse pressure-gradient flows.

The freestream dependency of the original Wilcox $k-\omega$ model has been investigated in detail in Ref. 22, and it has been shown that the magnitude of the eddy viscosity can be changed by more than 100% just by using different values for ω_f . This is clearly unacceptable, and corrections are necessary to insure unambiguous solutions. The standard $k-\omega$ model developed by Wilcox has been modified in Ref. 9 so that the computed solutions are insensitive to the freestream values of ω_f . This modified model is called baseline (BSL) $k-\omega$ model. The BSL $k-\omega$ model was further modified⁹ to improve the predictions of strong adverse pressure gradient separated flows; this model is called shear stress transport (SST) $k-\omega$ model. In this paper, the SST $k-\omega$ turbulence model will be extensively tested for unsteady flows. This model has been tested in Ref. 9 for a wide class of steady separated flows and has shown good agreement with experiments.

Results and Discussion

The main objective of the present investigation is to assess the accuracy of one- and two-equation turbulence models for the computation of unsteady, massively separated, high Reynolds-number airfoil flows. Experimental measurements for dynamic stall are usually available in the form of unsteady loads (lift coefficient C_l , drag coefficient C_d , and pitching moment coefficient C_m). Accurate computation of these quantities for unsteady flow is important and usually is sufficient for engineering and design applications. Sometimes unsteady surface pressures are also reported.

To confirm that the turbulence models under consideration had been implemented correctly, computations were first performed for a standard incompressible airfoil test case²³ with trailing-edge separation. Solutions over the NACA-4412 airfoil are obtained at $\alpha = 13.87$ deg angle of attack and $Re_c = 1.52 \times 10^6$. In the experiment of Ref. 23, the measurements are obtained for low-speed incompressible flow. Here, the solutions with different turbulence models are obtained at $M_\infty = 0.2$. A 241×91 point grid is used for the numerical solution. The surface pressure coefficients computed with different models show only small differences with the measurements in the trailing-edge region. The computed velocity profiles at various streamwise locations are compared with the measured values in Fig. 1. The B-B model overpredicts separation, and the S-A model yields less separation compared with the experiment. The $k-\epsilon$ and the $k-\omega$ models predict attached flow. The SST $k-\omega$ model predicts the separation and profile shape fairly well. The solutions computed with different models have been converged to an average residual based on density to order 10^{-12} and a maximum residual to order 10^{-6} . The trends observed for this separated flow at a fixed angle of attack carry over to the unsteady case and help to interpret the computed unsteady results.

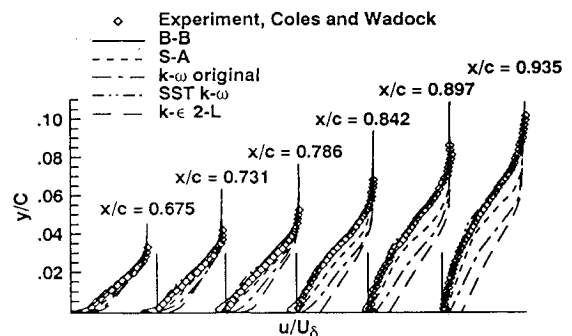


Fig. 1 Comparison of the computed and measured boundary-layer profiles with the experiment of Ref. 24 for $x/c = 0.675, 0.731, 0.786, 0.842, 0.897, \text{ and } 0.935$; $\alpha = 13.87$ deg, and $Re = 1.52 \times 10^6$.

Fully Turbulent Tripped Unsteady Flows

For validation of unsteady, fully turbulent solutions, the experimental measurements of Ref. 24 for a NACA-0015 airfoil are used, because in this experiment, as opposed to that of Ref. 13, the boundary layer was tripped at the leading edge to ensure a fully turbulent boundary layer for attached, light-stall and deep-stall cases. Oscillatory motions at sufficiently high angles of incidence include both massive separation during the upstroke and flow reattachment during the downstroke. The freestream Mach number is $M_\infty = 0.3$, and the Reynolds number, based on the airfoil chord length, is $Re_c = 2 \times 10^6$. In the experiment the flow was tripped at the leading edge, and it is expected that the surface flow is fully turbulent. The airfoil oscillates as $\alpha(t) = \alpha_m + \alpha_a \sin(\omega t)$ with a reduced frequency $k = 0.1$. The oscillation amplitude remains fixed at $\alpha_a = 4.2$ deg, and variation of the mean angle α_m leads to different flow regimes. Attached flow corresponds to $\alpha_m = 4$ deg. The light- and deep-stall regimes are obtained for $\alpha_m = 11$ and 15 deg, respectively.

The computations use a C-type 311×91 point grid with 130 points on the suction side and 45 points in the wake having a grid spacing $dz = 0.00001$ chord lengths away from the airfoil surface as baseline grid. Normal spacing of $0.00001c$ yields a $y^+ \approx 2$ for the first grid point above the suction side surface. A 421×151 points grid with increased resolution in the normal to the wall separated flow region and reduced normal grid spacing of $dz = 0.000005$ is also used. This grid has 111 points on the pressure side and 221 points on the suction side. Two oscillatory cycles are computed because for all cases it was found that the third cycle is always identical to the second cycle. Different numbers of time steps for a cycle were tested, and it was found that computations with 10,000, 16,000, and 40,000 time steps gave identical solutions. The results presented are obtained using 16,000 time steps, which correspond to a nondimensional time step $\Delta t \approx 0.0065$ or a maximum Courant number $Cu \approx 700$. The performance of all turbulence models is evaluated for the deep-stall case. For the light-stall case, solutions are computed only with the B-B, S-A, and SST $k-\omega$ turbulence models, and a grid-resolution study is performed. The attached unsteady flow case is computed with the B-B and the SST $k-\omega$ models only.

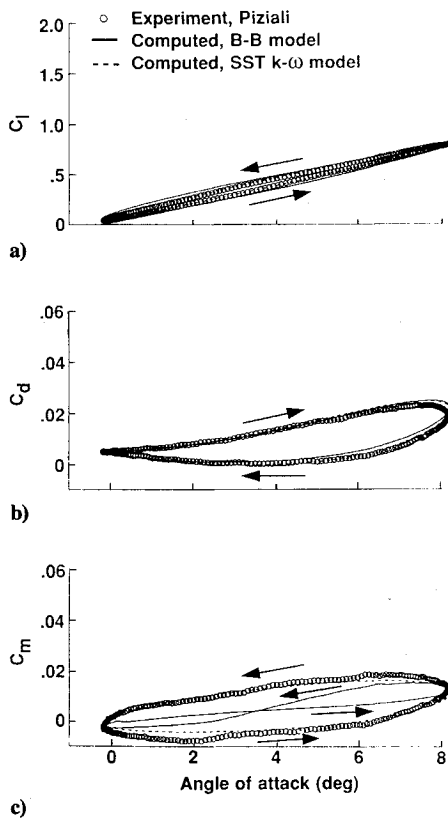


Fig. 2 Hysteresis effects for attached flow: $M = 0.3$, $\alpha(t) = 4 \text{ deg} + 4.2 \text{ deg} \sin(t)$, $k = 0.1$, and $Re = 2 \times 10^6$.

$$\alpha(t) = 4 \text{ deg} + 4.2 \text{ degsin}(t)$$

This flow is essentially attached, and it is computed only with the B-B and SST $k-\omega$ models. Comparisons of the computed hysteresis loops with the experiment (Fig. 2) show that the loads computed with the SST $k-\omega$ model are in good agreement with the experiment. The lift computed with the B-B model overpredicts the experimental values, and the pitching moment hysteresis does not agree with the experiment. The computed drag, however, is in agreement with the experiment. Comparison of the unsteady surface pressure coefficients computed by the two models shows that the lift and pitching moment disagreements are not caused by large differences of the computed unsteady surface pressures.

$$\alpha(t) = 11 \text{ deg} + 4.2 \text{ deg} \sin(t)$$

The computed solutions show that this flow is characterized by moderate trailing-edge separation that develops at the peak of the cycle. The flow remains separated for a large portion of the downstroke, and a recirculatory region of about half a chord length is observed. As a result, more significant hysteresis effects than the previous case are obtained. The hysteresis loops obtained from solutions using the baseline grid with the B-B, S-A, and SST $k-\omega$ turbulence models are compared with the experimental data in Fig. 3. The B-B model predicted the most separation and yields a lower lift during reattachment, but it gives good predictions for drag and pitching moment coefficients. The S-A model predicts the least separation and shows earlier flow reattachment. Similar to the S-A model, the SST $k-\omega$ model, even though it shows closer agreement with the experimental lift during the initial part of the downstroke, predicted more rapid lift recovery. A solution computed on the refined 421×151 point grid with the SST $k-\omega$ turbulence model and the baseline grid solution showed little grid sensitivity. The lift and pitching moments obtained from the refined grid solution are virtually the same with the baseline grid solution. The predicted drag is the same for the upstroke and shows a maximum improvement of about 5% during the downstroke.

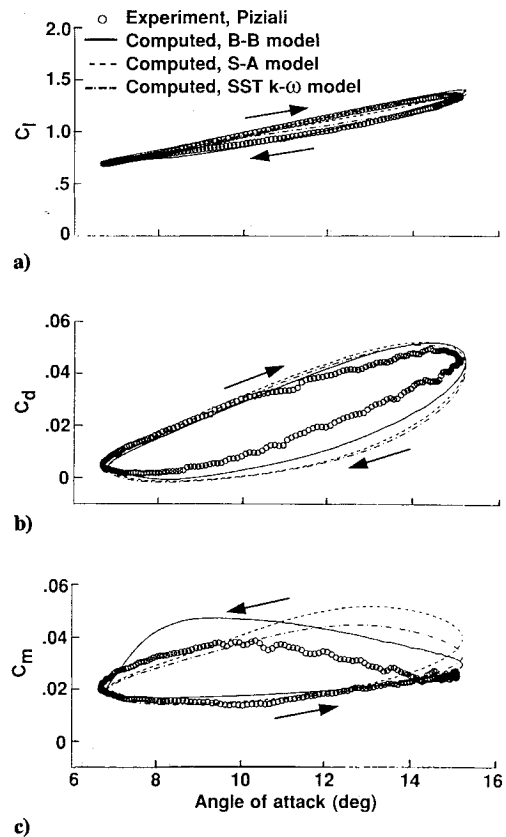


Fig. 3 Hysteresis effects for light-stall flow: $M = 0.3$, $\alpha(t) = 11 \text{ deg} + 4.2 \text{ deg} \sin(t)$, $k = 0.1$, and $Re = 2 \times 10^6$.

$$\alpha(t) = 15 \text{ deg} + 4.2 \text{ deg} \sin(t)$$

The computed solution shows that this unsteady flowfield is characterized by massive flow separation that develops before the peak angle of incidence. The unsteady flowfield structure is illustrated in Fig. 4 at the peak and mean angle of attack during the downstroke. In this figure trajectories are obtained from particles that are released continuously at various locations and then convected in time through the flowfield. Snapshots of this particle animation at peak and mean incidence are shown in Fig. 4. At peak incidence, $\alpha = 19.2$ deg, and before the downstroke, the primary vortex is ready to shed and a secondary trailing-edge vortex has formed. Shedding of the primary vortex causes decrease in lift and pitching moment. The flow remains separated for a large part of the downstroke, and significant hysteresis effects are obtained. Figure 4b shows that a large region of the flowfield remains separated when the mean angle of attack, $\alpha = 15.0$ deg, during downstroke is reached. It is a challenge for turbulence models to be able to capture flow separation and reattachment and yield good quantitative predictions for these kind of flows. The lift, drag, and pitching moment hysteresis loops obtained from computations with the B-B and S-A one-equation turbulence

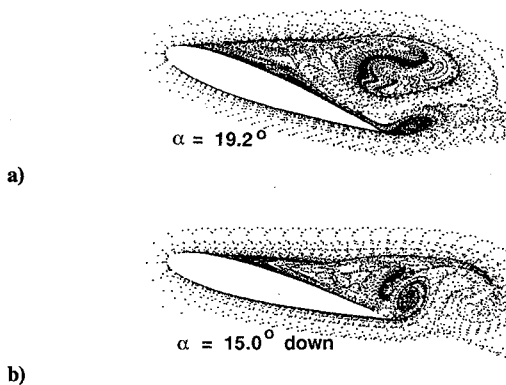


Fig. 4 Vortical flowfield development shown by convected particles: a) $\alpha = 19.2$ deg and b) $\alpha = 15.0$ deg down; $M = 0.3$, $\alpha(t) = 15 \text{ deg} + 4.2 \text{ deg} \sin(t)$, $k = 0.1$, and $Re = 2 \times 10^6$.

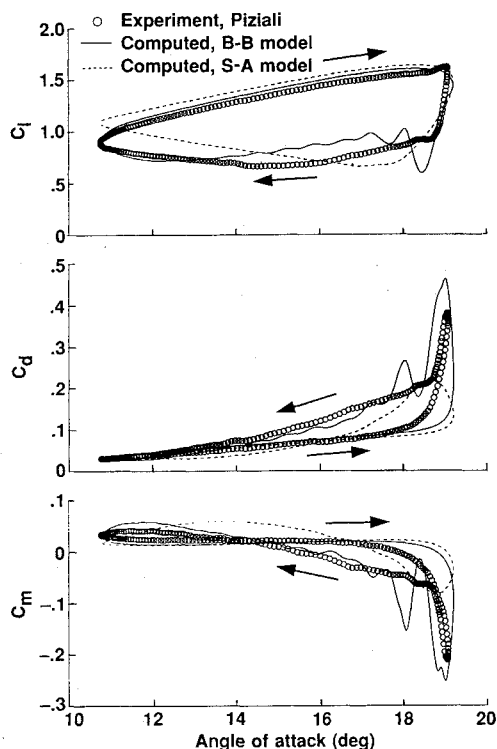


Fig. 5 Hysteresis effects for deep stall obtained with one-equation models: $M = 0.3$, $\alpha(t) = 15 \text{ deg} + 4.2 \text{ deg} \sin(t)$, $k = 0.1$, and $Re = 2 \times 10^6$.

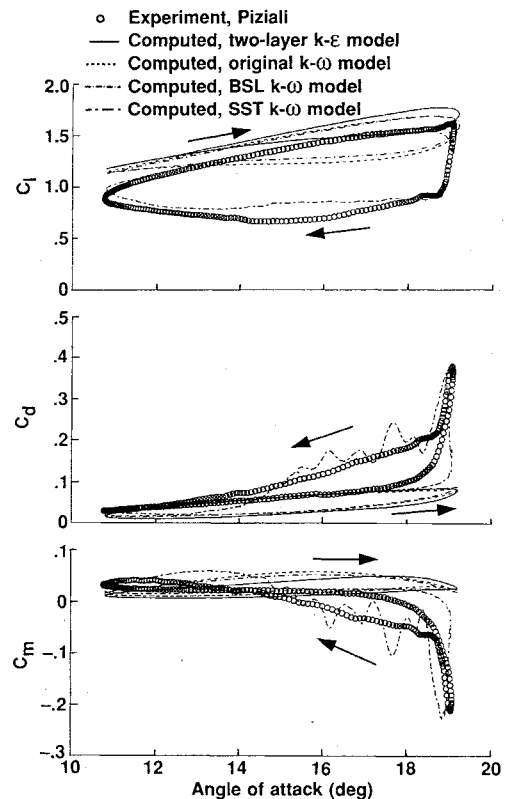


Fig. 6 Hysteresis effects for deep stall obtained with two-equation models: $M = 0.3$, $\alpha(t) = 15 \text{ deg} + 4.2 \text{ deg} \sin(t)$, $k = 0.1$ and $Re = 2 \times 10^6$.

models are compared with the experiment in Fig. 5. The lift hysteresis is predicted reasonably well by both models. The drag and pitching moment hysteresis loops indicate that both models delay onset of separation. The loads computed with the B-B model show oscillatory behavior at the downstroke. The B-B model predictions are in closer agreement with the experiment. A smaller extent of separated flow is obtained with the S-A model, resulting in smaller extreme values of drag and pitching moment. A more rapid flow reattachment was also observed.

Predictions of hysteresis loops obtained from solutions with the two-equation turbulence models are compared with the experiment in Fig. 6. The $k-\epsilon$, the original $k-\omega$, and the BSL $k-\omega$ (where the freestream dependency is removed) did not yield enough separation. Therefore, the loads computed with these models significantly deviated from the experimentally measured values. The solution obtained with the SST $k-\omega$ model shows large flow separation, and the predictions are in close agreement with the experiment. However, at large angles of incidence and during the downstroke the loads show again oscillatory behavior.

Solutions computed with the B-B and SST $k-\omega$ models show development of a trailing-edge vortex at the end of the pitch-up motion. During the downstroke this vortex convects in the wake, and another trailing edge vortex forms. The second vortex initially grows in size and then convects in the wake, and the vortex shedding repeats. During the downstroke the trailing-edge vortex shedding causes oscillations to the loads. The computed solutions for this part of the cycle are sensitive to grid distribution at the trailing edge and the wake region.

The unsteady solutions follow the trends of the steady results. The B-B model has the tendency to predict the most separation following the SST $k-\omega$ model. The S-A model tends to underpredict the amount of separation but not nearly to the degree of the standard $k-\omega$ and $k-\epsilon$ models. To put the results in better perspective, the pitching moments for all three oscillatory cases are plotted to the same scale in Fig. 7 and compared with the B-B and SST $k-\omega$ model solutions. The drag and pitching moment variation for the deep-stall case is an order of magnitude larger compared with the variation in

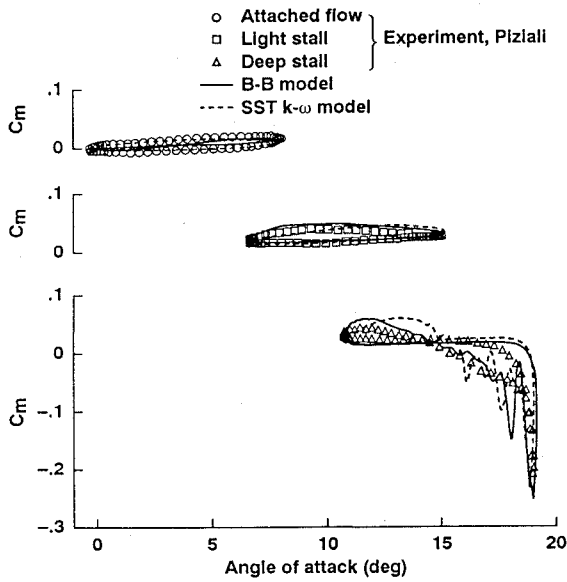


Fig. 7 Effect of increased mean angle on pitching moment.

the attached flow and the light-stall flow cases. As seen in Fig. 7, the discrepancies between experiment and computation for the attached and light-stall cases are very small in relation to those for the deep-stall case.

Effect of Transition

A light-stall case from the experimental results reported in Ref. 13 is chosen to demonstrate the effect that leading-edge transition can have on the development of the unsteady flowfield. In Ref. 13, measurements in the form of integrated aerodynamic loads (C_l , C_d , C_m) have been reported for a wide range of flow conditions and airfoil shapes. In addition, unsteady surface pressure coefficients are given. In contrast to the NACA-0015 experiment of Ref. 24, in Ref. 13 boundary-layer trips were used only for a limited number of deep-stall cases. Unsteady solutions are obtained for a NACA-0012 airfoil executing harmonic motion $\alpha(t) = 10 \text{ deg} + 5 \text{ deg} \sin(\omega t)$, with a reduced frequency $k = 0.1$, and $M_\infty = 0.3$ with untripped flow of a Reynolds number $Re_c = 4.0 \times 10^6$. The same case was also considered in Refs. 10 and 11. However, because significant hysteresis effects were not obtained for the experimental maximum angle of incidence, the amplitude of the oscillation or the mean angle was slightly increased for the computation. As a result, in both investigations a maximum angle of attack larger than $\alpha_{max} = 15 \text{ deg}$ reported by the experiment was reached. Experimental uncertainties and tunnel wall interference effects justified this alteration of the experimental conditions. Another reason why the maximum angle of incidence had been increased was to promote separation predicted by the turbulence models. Hysteresis effects were obtained at these larger angles of incidence, and it was concluded that massive flow separation at the trailing edge alone was responsible for stall.

Fully turbulent flow simulations of the previous section have demonstrated that the B-B model produces the most separation. The S-A model produces less separation compared with the B-B and the SST $k-\omega$ models. The B-B and the SST $k-\omega$ models yield similar predictions, but the B-B model is more computationally efficient. Therefore, this case is solved only with one-equation models. A solution obtained with the B-B model (Fig. 8), which produces the most separation, for the same oscillation amplitude as the experiment¹³ still did not yield significant hysteresis effects. In addition, a counterclockwise loop for the pitching moment, as opposed to the clockwise loop shown in the experiment, was obtained. The same procedure of Refs. 10 and 11 was followed again, and the oscillation amplitude was "arbitrarily" increased. A solution with the B-B model was obtained with an oscillation amplitude of 5.3 deg. For the S-A model, which yields less separation, the oscillation amplitude was further increased to 5.5 deg. The computed lift and pitching moment hysteresis (Fig. 8) showed reasonable agreement with the experiment. The computed drag, even though it followed

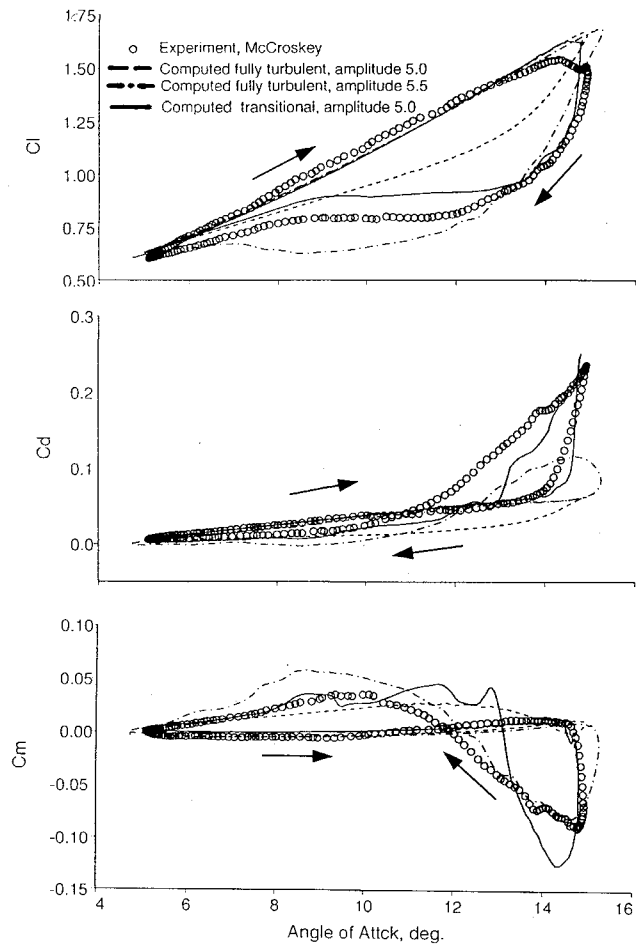


Fig. 8 Effect of leading-edge transition on hysteresis effects: $M = 0.3$, $\alpha(t) = 10 \text{ deg} + 5 \text{ deg} \sin(t)$, $k = 0.1$, and $Re = 4 \times 10^6$.

the experimental trends, underpredicted the extreme measured drag values. It was also observed that the phase angle, where the computed drag and nose-down pitching moment increased, lagged the experimental values by approximately 1 deg. Comparison of the measured unsteady surface pressure measurements with the computed surface pressure indicated that large discrepancies occurred on the suction side and that the agreement of the lift and the pitching moment with the experiment was coincidental.

Careful observation of the experimental surface pressure measurements shows that the lift drop, the increases in drag, and nose-down pitching moment are associated with a drop in the leading-edge suction peak. This suction pressure drop occurs because of leading-edge flow separation. The two physical mechanisms that can force the flow to separate at the leading-edge are either a shock or laminar/transitional flow behavior. The progressive drop of the suction peak shown in the experiment does not support the shock separated flow assumption. Therefore, there is an indication that, even though the Reynolds number is large, the leading-edge flow could be transitional. A rough approximation of the transitional flow behavior at the leading edge is performed with the following procedure. The transition onset is specified to occur immediately downstream of the suction peak location. The flow from the stagnation point until the transition onset is computed as laminar. The production term of the one-equation B-B model is set equal to zero for the laminar region. As a result, the model yields an eddy viscosity of almost zero for the laminar region. Beyond the transition point, the full-production term is utilized, and the computed eddy viscosity rapidly increases downstream from the transition point until a fully turbulent value is reached.

A 351×91 point grid with 170 points on the suction side is used for the numerical solution. This grid has refined resolution at the leading-edge region. In the computed solutions the transitional flow region extends only over a few streamwise computational cells. A

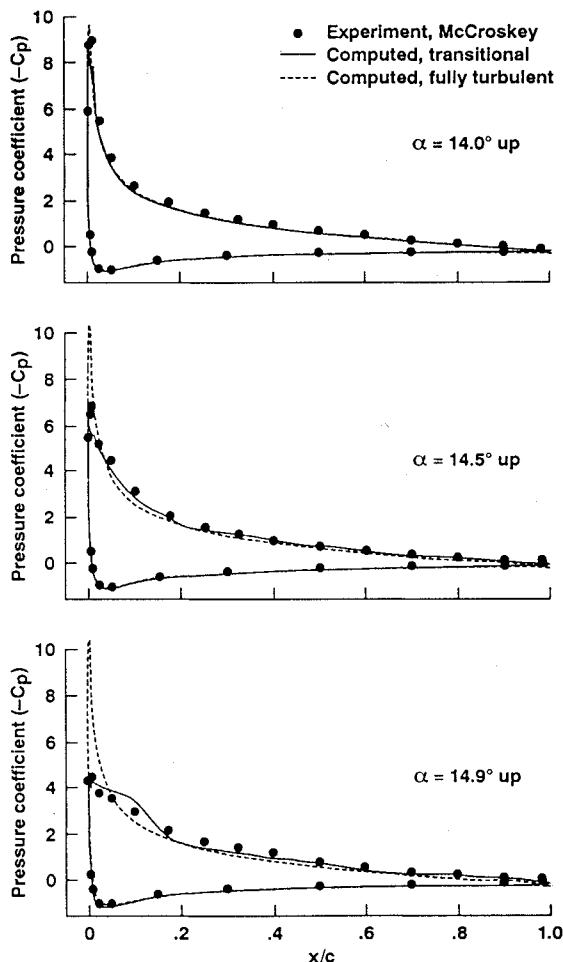


Fig. 9 Effect of transition on the computed surface pressure coefficient: $M = 0.3$, $\alpha(t) = 10 \text{ deg} + 5 \text{ deg} \sin(t)$, $k = 0.1$, and $Re = 4 \times 10^6$.

leading-edge separation bubble forms at approximately 14 deg during the upstroke and increases significantly in size before the peak of the cycle. The loads obtained from the laminar/transitional/turbulent flow solutions are compared with the experiment in Fig. 8. For comparison, the loads obtained from a fully turbulent solution are shown in the same figure. The lift hysteresis loop (Fig. 8a) shows good qualitative agreement with the experiment. Good quantitative agreement is obtained for the upstroke, but a more rapid lift recovery during part of the downstroke is observed. Similar trends are shown for the drag and pitching moment. It appears that the transitional solution predicts a more rapid flow reattachment. However, there is good agreement with the experiment for the computed nose-down pitching moment and drag increase attributed to the massively separated flow during the initial part of the downstroke. It is also significant that the extreme values of the drag and pitching moment are closely predicted and the computed loads do not lag the experiment. Discrepancies obtained for the downstroke are caused by uncertainties in transition modeling and deficiencies of the turbulence model.

The surface pressure coefficient distributions for three angles during the upstroke, $\alpha = 14.0$, 14.5 , and 14.9 deg, obtained from the fully turbulent and the transitional computations are compared with the measured values in Fig. 9. At $\alpha = 14.0$ deg (Fig. 9a) both the fully turbulent and the transitional solutions are in agreement with the experiment for the region near the leading edge. The fully turbulent solution, however, slightly overpredicts the suction peak. The surface pressure distribution obtained from the transitional solution is in close agreement with the experiment and shows the development of a leading-edge separation bubble. A very small region of transitional flow is found. As the angle of attack increases to $\alpha = 14.5$ deg, the experiment shows a large drop in the suction peak caused by flow separation. Visualization of the computed velocity fields shows that only trailing-edge separation was obtained for the fully turbulent computation. The transitional solution, on the other

hand, yields more separated flow and shows formation of a vortex like structure. At $\alpha = 14.9$ deg, which is the peak angle of attack of the experiment, the suction peak is further diminished and the vortical structure generated at the leading edge is convected downstream. At this angle the fully turbulent solution does not agree with the experiment and shows further increase of the suction peak. It appears that the transitional solution properly captures the physical mechanism observed in the experiment and shows development of a leading-edge, vortical, dynamic-stall-like structure as the computed surface pressure coefficient demonstrates.

The values of lift and pitching moment obtained from the turbulent solution with an increased oscillation amplitude are coincidentally close to the measured values. The computed drag coefficient, however, disagrees with the experiment. Therefore, it is necessary to always compare lift, drag, and pitching moment coefficients, when surface pressure measurements are not available. The fully turbulent solution predicts attached leading-edge flow and trailing-edge separation. The transitional solution predicts a leading-edge vortex-like structure and larger overall separation compared with the fully turbulent solution. The leading-edge flow development affects significantly the suction surface flowfield and results in larger overall separation. The leading-edge vortical structure is not the same as a classical dynamic stall vortex, which is clearly observed in both experiments and computations for larger oscillation amplitudes or different pitch rates. This structure forms at about 14 deg during the upstroke and bursts in the boundary layer. Around the peak angle of the cycle a rapid progression of the trailing-edge separation towards the leading edge is also observed.

As an approximate location for the transition onset, the maximum suction pressure point is used. For high-Reynolds-number flow, the transitional region is small. It appears that the approach, where an approximate transition onset location is determined based on the maximum suction pressure, and a simple transition model that yields an "effective" eddy viscosity for the transitional region is used, does not significantly degrade the solution for the pitch-up part of the cycle. It is not expected that these rough approximations allow accurate modeling of the complex physical mechanisms of transition, bubble formation, and reattachment. It is demonstrated, however, that transition plays a significant role in the development of the unsteady separated flowfield.

Conclusions

An evaluation of the ability of one- and two-equation turbulence models in predicting hysteresis effects of unsteady fully turbulent flow over oscillating airfoils in the light- and deep-stall regime was conducted. It appears that turbulence models that tend to suppress separation perform poorly. Even though none of the models considered in this investigation are capable of accurately predicting the deep-stall case, the B-B, the S-A, and the SST $k-\omega$ models show a significant improvement over standard two-equation models. For the light-stall case the S-A model did not yield sufficient separation and underpredicted the extreme values of the unsteady loads. The B-B model overpredicted the lift drop for the light-stall case and the attached flow cases. The standard $k-\epsilon$ and the $k-\omega$ models did not predict separation even for the deep-stall case. The SST $k-\omega$ model gave good predictions for the attached and the light-stall cases.

It was found that the leading-edge transitional flow is of primary importance to the overall development of the unsteady flowfield, if the flow is not tripped at the leading edge. A laminar/transitional leading-edge separation bubble developing during the pitch-up motion produces a dynamic-stall-like vortical structure. It was shown that a simple transition model significantly improves the predictions. However, accurate methods for transition modeling and prediction are still required.

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